

# Algorithms

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## M/R Algorithms

### Basic Algorithms

#### Addition

#### Addition of multiple matrices

- <https://issues.apache.org/jira/browse/HAMA-154>

#### Multiplication

- Iterative Approach

```
For i = 0 step 1 until N -1
  Job: Computes the ith row of C = Matrix-Vector multiplication

Iterative job:

- A map task receives a row n of B as a key, and vector of row as its value
- Multiplying by all columns of ith row of A
- Reduce task find and add the ith product

1st
+           +   +
| a11 a12 a13 | | a11 a21 a31 |
| ... ... ... | X | a12 a22 a32 |
| ... ... ... | | a13 a23 a33 |
+           +   +

2nd
+           +   +
| ... ... ... | | a11 a21 a31 |
| a21 a22 a23 | X | a12 a22 a32 |
| ... ... ... | | a13 a23 a33 |
+           +   +
....
```

- Blocking Algorithm Approach

To multiply two dense matrices A and B, We collect the blocks to 'collectionTable' firstly using map/reduce. Rows are named as  $c(i, j)$  with sequential number  $((N^2 * i) + ((j * N) + k))$  to avoid duplicated records.

CollectionTable:

	matrix A	matrix B
block(0, 0)-0	block(0, 0)	block(0, 0)
block(0, 0)-1	block(0, 1)	block(1, 0)
block(0, 0)-2	block(0, 2)	block(2, 0)
... N	...	
block(N-1, n-1)-(N^3-1)	block(N-1, N-1)	block(N-1, N-1)

Each row has a two sub matrices of a(i, k) and b(k, j) so that minimized data movement and network cost.

Blocking jobs:

Collect the blocks to 'collectionTable' from A and B.

- A map task receives a row n as a key, and vector of each row as its value
- emit (blockID, sub-vector) pairs
- Reduce task merges block structures based on the information of blockID

Multiplication job:

- A map task receives a blockID n as a key, and two sub-matrices of A and B as its value
- Multiply two sub-matrices:  $a[i][j] * b[j][k]$
- Reduce task computes sum of blocks
- $c[i][k] +=$  multiplied blocks

## Matrix Norm

- Find the maximum absolute row sum of matrix

Matrix.Norm.One is that find the maximum absolute row sum of matrix. Comparatively, it's a good fit with MapReduce model because doesn't need iterative jobs or table/file JOIN operations.

The maximum absolute row sum =  $\max_{1 \leq i \leq n} \left( \sum_{j=1}^{j=n} |a_{\{i,j\}}| \right)$

- A map task receives a row n as a key, and vector of each row as its value
- emit (row, the sum of the absolute value of each entries)
- Reduce task select the maximum one

NOTE: Matrix.infinity, Matrix.Maxvalue and Matrix.Frobenius are almost same with this.

## Compute the transpose of matrix

The transpose of a matrix is another matrix in which the rows and columns have been reversed. The matrix must be square for this work.

+		+	+		+					
	a11	a12	a13		=>	a11	a21	a31		
	a21	a22	a23				a12	a22	a32	
	a31	a32	a33				a13	a23	a33	
+		+	+		+					+

- A map task receives a row n as a key, and vector of each row as its value
- emit (Reversed index, the entry with the given index)
- Reduce task sets the reversed values

## Compute the determinant of square matrix

- <http://issues.apache.org/jira/browse/HAMA-66>

## **Decomposition Algorithms**

### **Cholesky Decomposition**

- <http://issues.apache.org/jira/browse/HAMA-94>

### **Singular Value Decomposition**

- <http://issues.apache.org/jira/browse/HAMA-176>